UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

International General Certificate of Secondary Education

MARK SCHEME for the May/June 2008 question paper

0580, 0581 MATHEMATICS

0580/04, 0581/04 Paper 4 (Extended), maximum raw mark 130

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began.

All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

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1 (a) (i)	250		B1	
(ii)	their (a)(i) \div 5×52 o.e.		M1	SC1 for $12.5 \div 5 \times 52$, implied by 130
(11)	2600 ft	www2	A1 ft	Series in the series, implies by the
(iii)	$\frac{their (a)(ii) - 2450}{2450} \times 100$ o.e. 6.1 (22) ft	www2	M1 A1ft	$\frac{\text{their (a)(ii)}}{2450} \times 100 - 100, \ \frac{2450}{100} = \frac{150}{x}$ ft M & A only if their (a)(ii) > 2450
(b) (i)	20 ÷ 5 × 3 12	www2	M1 A1	Accept 12, 8 or 8, 12
(ii)	their (b)(i) \div 3 and (20 – their (b)(i))		M1	4 and 3.2 or 7.2 or 7h 20 mins seen imply M1
	7 hours 12 mins cao	www2	A1	Condone poor notation e.g. 7-12
(iii)	2.78 (2.777–2.778) o.e. cao o.e. in other units		B1	o.e. must have units stated e.g. 0.7716m/s, 46.29 – 46.30 m/min
(iv)	16 07 o.e. ft		B1 ft	ft their (b)(ii) + 08 55 iff finishes on same day and (b)(ii) has hours and mins
(c)	$20 \times 100000 \div 80$ o.e.		M1	
	25 000 or 2.5 ×10 ⁴	www2	A1	25 000 seen in final ans. After M0, SC1 for figs 25 or 0.00004 final answer [13]

			10r 11gs 23 or 0.00004 final answer
2 (a) (i)	(x+4)(x-5)	B2	If B0, SC1 if of form $(x \pm 4)(x \pm 5)$,
(ii)	-4, 5 ft	B1 ft	Only ft the SC
			-4, and 5 not from $(x-4)(x+5)$. B1 for $(-2)^2$ -4(3)(-2) (or better) seen
(b)	$-(-2) + \sqrt{(-2)^2 - 43 - 2}$		B1 for $(-2)^2$ –4(3)(-2) (or better) seen
	$\frac{-(-2) \pm \sqrt{(-2)^2 - 4.3 - 2}}{2.3}$	B1,B1	inside a square root.
	2.3		The expression must be in the form
			$\frac{p + (\text{or} -)\sqrt{q}}{r} \text{ then } \mathbf{B1} \text{ for } p = -(-2) \text{ and}$
			then B1 for $p = -(-2)$ and
			22 1 4
			r = 2.3 or better
			Allow recoveries from incomplete lines
	0.55 1.22	D1 D1	If DO SC1 for 0.5 and 1.2 or both
	-0.55, 1.22 cao	B1,B1	If B0, SC1 for –0.5 and 1.2 or both answers correct to 2 or more decimal
			places (rounded or truncated).
			-0.54858, 1.21525
(a) (i)	(m-2n)(m+2n)	B1	-0.34636, 1.21323
(c) (i) (ii)	-12	B1	
(iii)	-12	DI	B1 for $(4x^2 + 6x + 6x + 9)$ or
(111)	20x + 5 o.e. cao final ans	B2	$(x^2 - x - x + 1)$ or
	20x + 5 o.c. cao imai ans	DZ	
(iv)	$4n^2 = m^2 - y$ o.e.	M1	$(2x+3-2(x-1))(2x+3+2(x-1))$ M1 for correct re-arrangement for n^2 term
(11)		1,11	(may be $-n^2$)
	$n^2 = \frac{m-y}{1}$ o.e.	M1	M1 for correct division by $4 \text{ or } -4$
	4	1,11	M1 for correctly taking square root of n^2
	$n^{2} = \frac{m^{2} - y}{4} \text{o.e.}$ $(n) = \sqrt{\frac{m^{2} - y}{4}} \text{o.e.}$ www3	M1	term
	$(n) = \sqrt{\frac{m}{4}} \text{o.e.} $ www3		
	Mark final answer		SC2 for $\sqrt{\frac{y \pm m^2}{4}}$ or $\sqrt{\frac{m^2 - y}{4}}$ o.e. ww
			V 4 V 4
(d) (i)	4 or -4 or ±4	B1	
(ii)	$n(m^4 - 16n^4)$ or	M1	Correctly taking out <i>n</i> or a correct factor
	$(m^2n - 4n^3)(m^2 + 4n^2)$ or		with <i>n</i> still in one bracket
	$(m^2n + 4n^3)(m^2 - 4n^2)$ or		
	$n(m-2n)(m+2n)(m^2+4n^2)$	A1	Must be final answer [17]

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3			Accept all probability answers as fractions (non-reduced or reduced), decimals or percentages. -1 once for 2 sf answers or correct words. Condone numerical errors in simplifying or converting after correct answers seen. Ratio answers score zero throughout.
(a) (i)	$\frac{1}{3}, \frac{3}{8}, \frac{6}{8}, \frac{2}{8}$ o.e.	В3	-1 each error bod if no letters given
(ii)	$\frac{2}{3} \times \frac{5}{8}$ $\frac{5}{12} \text{ o.e.} \qquad \text{www2}$	M1 A1	$\frac{10}{24}$, etc., 0.416(6)
(iii)	their $\frac{5}{12} + \frac{1}{3} \times \frac{6}{8}$ $\frac{2}{3} \text{ o.e. cao} \qquad \text{www2}$	M1 A1	$\frac{16}{24}$, $\frac{8}{12}$, etc., 0.666(6)
(b) (i)	$\frac{3}{10} \times \frac{2}{9} \times \frac{1}{8}$ $\frac{1}{120} \text{ o.e.} \qquad \text{www2}$	M1 A1	$\frac{6}{720}$, etc., 0.00833(3)
(ii)	$\frac{119}{120}$ o.e.	B1ft	$\frac{714}{720}$, etc., 0.991(6) ft 1 – their (i) not for 7/10 Could start again and have a correct answer independently [10]
4 (a) (i)	36 (36.0–36.4)	B1	

4 (a) (i)	36 (36.0–36.4)	B1	
(ii)	50 (50.0–50.4)	B1	
(iii)	29 (28.6–29.4)	B1	
(iv)	20	B2	If B0, SC1 for 19 or 21 or 180 seen
(b) (i)	p = 16, q = 4	B1,B1	If B0, SC1 if p and q add up to 20
(ii)	$\left(\frac{7220}{200}\right) = 36.1$ cso www4	B4	Answer 36 scores 4 marks after some correct working shown with no incorrect working seen M1 for using mid-values at least four correct from 5, 15, 25, 35, 45, 55, 65, 75 M1 (dep on correct mid values or mid-values ± 0.5) for $\sum fx$ (at least four correct products) M1 (dependent on 2^{nd} M1) for dividing sum by 200 or 180 + their p + their q
(c)	8.2 (8.19–8.20), 11.4 , 5 (5.00–5.01)	B4	B3 for 2 correct or B2 for 1 correct After B0, SC2 for fd's 2.7(3) o.e.,
5 (a) (i)	$360 \div 8$ or $(8-2) \times 180$	M1	3.8 o.e, 1.6(6) o.e. or SC1 for 2 of fd's correct (15) allow 6×180

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	$180 - \text{their } (360 \div 8) \text{ o.e.} \qquad \div 8$	M1	dependent
(ii)	45° used or use implied o.e.	E1	Accept sketch with values
(b) (i)	l 45	M1	For o.e. allow implicit expression
	$\frac{l}{12} = \cos 45$ o.e.		
	(PH =) 8.49 (8.485) www2	A1	Accept $\sqrt{72}$, $2\sqrt{18}$, $3\sqrt{8}$, $6\sqrt{2}$
(ii)	$(PQ =) 2 \times \text{their } PH + 12 \text{ o.e.}$	M1	
	(<i>PQ</i> =) 29.(0) (28.96–29.00) ft www2	A1 ft	ft their PH accept surd form
(iii)	their $PH \times \text{their } PH \div 2$ o.e.	M1	
	(Area <i>APH</i> =) 36 (35.95–36.1) ft www2	A1 ft	ft their PH
(iv)	$(\text{their } PQ)^2 - 4 \times \text{their area of triangle o.e.}$	M2	If M0, M1 for a clear collection of areas
	(Area octagon =) 695 (694.0–697.1) cao		leading to the octagon possibly without
	www3	A1	any calculation shown
(c) (i)	0.5 of their PQ o.e.	M1	e.g. $6 + PH$, $6 \tan 67.5^{\circ}$
	14.5 (14.47–14.53) cao www2	A1	accept surd form
(ii)	$\pi \times (their r)^2$	M1	(660.5)
	their circle area_×100	MI	D
	their octagon area	M1	Dependent on first M1 and circle smaller
			than the octagon
	94.8 (94.35 to 95.60) cao www3	A1	[17]

6 (a) (i)	$\begin{pmatrix} 2 \\ 1 \end{pmatrix}$	B1	Allow (2 1), condone omission of brackets
(ii)	$\begin{pmatrix} 2 \\ 1 \end{pmatrix}$ ft	B1ft	Allow (2 1), condone omission of brackets ft their (i) if a vector
(b)	Translation $\begin{pmatrix} 0 \\ -4 \end{pmatrix}$ o.e.	B1, B1	Allow (0 –4), condone omission of brackets, allow in words Any extra transformation spoils both marks
(c)	y > 0 o.e. x < 2 o.e. $y > \frac{1}{2}x$ o.e. y < 2x + 4 o.e.	B1 B1 B1 B2	For all four, condone strict inequalities and only penalise first incorrect sign, which may be = or an inequality sign If B0, B1 for $2x$ or for 4 if other co-efficient is not zero $y < \frac{1}{2}x + 4$ gets zero [9]

7 (a) (i)	cyclic	B1	Condone concyclic
(ii)	Any one of 40 , 45 , 50	B 1	Angle $BCT = 40^{\circ}$ is inconsistent with ST
	Any one of 20 , 25 , 30	B 1	parallel to OB. So different values of
	Any one of 105 , 110 , 115	B 1	angles x, y, z, OCT and AOC can be
			arrived at, depending on route taken.
(iii)	Any one of 80, 85, 90	B1	
(iv)	Any one of 210 , 215 , 220 , 225 , 230	B 1	
(b) (i)	Similar (or enlargement)	B 1	
(ii)	$\left(\frac{7}{10}\right)^2$ or $\left(\frac{10}{7}\right)^2$ o.e. seen	M1	(0.49), (2.04)
	9.8 (9.79 to 9.81) ww	w2 A1	It is possible to do (iii) then (ii) and full marks can still be scored
(iii)	1	M1	
	$\frac{1}{2} \times 10 \times height = 20$	A1	
	4 ww	w2	[11]

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8 (a)		M1	M1 for method of compound interest used
()	108 (.16) (allow 108.2(0)) www2	A1	1
(b)	148(.02) 324(.3)	B1 B1	
(c)	Correct axes full domains	S1	Condone absence of labels
	5 correct pts 100, 148 ft, 219, 324ft, 480	P3ft	P2ft for 4 correct, P1ft for 3 correct
			Points must be in correct square vertically,
			including on line
	Smooth exponential curve, correct shape	C 1	Scale error – remove that part and try to
	through 5 points		mark the rest
(d) (i)	265 – 270	B1ft	If out of range, then ft their graph at 25
			years
(ii)	17 or 18 cao	B 1	
(e) (i)	$(100) \times 7 \times 20$		
	(100) o.e.	M1	
	$100 + 7 \times 20$ or better	E 1	No errors
(ii)	380	B1	
(iii)	Correct straight ruled line for x – range 0 to	L2	P1ft for 2 of (0,100), (20,240) (40,380)ft
, ,	35		correctly plotted
(f)	27 – 29 cao	B1	[17]

9 (a) (i)	p + r	B1	Answers in bracketed column form penalise only once throughout
(ii)	$-\mathbf{p} + \mathbf{r}$	B1	
(iii)	$-\mathbf{p} + \frac{2}{3}\mathbf{r}$	B1	
(iv)	$\mathbf{p} + \frac{1}{2}\mathbf{r}$	B1	
(b) (i)	$\frac{3}{2} \times (-\mathbf{p} + \frac{2}{3}\mathbf{r}) \text{ or } -\frac{3}{2}\mathbf{p} + \mathbf{r} \text{ isw after}$ correct answer seen	B1 ft	ft only $\frac{3}{2}$ × their (a)(iii)
(ii)	$\overrightarrow{QP} + \overrightarrow{PS}$ o.e.	M1	o.e. is any correct route of at least 2 vectors
	$-\frac{3}{2}\mathbf{p}$ www 2	A1 ft	ft their $(b)(i) - r$
(c)	lie on a straight line	B1	dependent on their (b)(ii) being a multiple of p [8]

10(a) (i)	4	B1	
(ii)	24	B1	
(b) (i)	x + 12, x + 14 o.e.	B1,B1	Any order ignore ref to g and i
(ii)	(x+14-x) and $(x+12-(x+2))$		x + 12 and $x + 14$ must be seen to be used
	14 – 10 or 14 – 12 + 2 or 4	E1	No errors seen
(iii)	(x+2)(x+12) - x(x+14)	B1	Subtraction can be implied later
	24	E1	Dep on B1 and no errors anywhere for the E mark
(c) (i)	4	B1	
(ii)	20	B1	
(d) (i)	4	B1	
(ii)	x + 2n o.e., $x + 2 + 2n$ o.e.	B1,B1	
(iii)	4 <i>n</i>	B1	Allow $4 \times n$, $n \times 4$, $n4$ [13]